Vieta's Formula in Cubic Equations

▸ Start

Start

Let

Start

Let α

Start

Let α, β

Start

Let α, β , γ

▸ Start

Let α, β , γ be the roots

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$$ax^3 + bx^2 + cx + d = 0$$

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$$\begin{cases} x^3 \\ \end{cases}$$

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$$\begin{cases} x^3 & - & (\alpha+\beta+\gamma) \\ & & \end{cases}$$

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$$\begin{cases} x^3 - (\alpha+\beta+\gamma)\, x^2 + (\alpha\beta+\beta\gamma+\gamma\alpha)x \\ \end{cases}$$

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$$\begin{cases} \alpha+\beta \end{cases}$$

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