

# Solving Quadratic Inequalities in Algebra

$$ax^2 + bx + c < 0 \quad (a > 0, b, c \in \mathbb{R})$$

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$$\text{Let } D = b^2 - 4ac$$

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$\therefore$  No solutions ( $\because b^2 - 4ac \leq 0$ )