

Euclid's Lemma

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$$a|bc$$

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$$a|bc \text{ and}$$

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Let a and b and c be given integers. If bc is divisible by a and the greatest common divisor of a and b is 1, then c is divisible by a .

$$a|bc \text{ and } \gcd(a, b) = 1$$

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Let a and b and c be given integers. If bc is divisible by a and the greatest common divisor of a and b is 1, then c is divisible by a .

$$a|bc \text{ and } \gcd(a, b) = 1 \Rightarrow$$

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$$a|bc \text{ and } \gcd(a, b) = 1 \Rightarrow a|c \quad \text{▶ proof}$$

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