

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

[ $\forall$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$[\forall \epsilon$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0]$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$



$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

( $\Rightarrow$ )

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

$(\Rightarrow)$

$$a < 0$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

$(\Rightarrow)$

$$a < 0 \Rightarrow$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

( $\Rightarrow$ )

$$a < 0 \Rightarrow [\exists \epsilon$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

( $\Rightarrow$ )

$$a < 0 \Rightarrow [\exists \epsilon > 0$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

( $\Rightarrow$ )

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t.}$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

( $\Rightarrow$ )

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

( $\Rightarrow$ )

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$



$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

$(\Rightarrow)$

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

$(\Rightarrow)$

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$a < 0$ , Let

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

$(\Rightarrow)$

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$a < 0$ , Let  $\epsilon$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

$(\Rightarrow)$

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0, \text{ Let } \epsilon = -a$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

$(\Rightarrow)$

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0, \text{ Let } \epsilon = -a, a + \epsilon$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

$(\Rightarrow)$

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0, \text{ Let } \epsilon = -a, a + \epsilon = a + (-a)$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

$(\Rightarrow)$

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0, \text{ Let } \epsilon = -a, a + \epsilon = a + (-a) = 0$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

$(\Rightarrow)$

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0, \text{ Let } \epsilon = -a, a + \epsilon = a + (-a) = 0 \leq 0$$



$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

( $\Rightarrow$ )

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0, \text{ Let } \epsilon = -a, a + \epsilon = a + (-a) = 0 \leq 0$$

( $\Leftarrow$ )

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

$(\Rightarrow)$

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0, \text{ Let } \epsilon = -a, a + \epsilon = a + (-a) = 0 \leq 0$$

$(\Leftarrow)$

$a$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

( $\Rightarrow$ )

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0, \text{ Let } \epsilon = -a, a + \epsilon = a + (-a) = 0 \leq 0$$

( $\Leftarrow$ )

$$a \geq 0$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

( $\Rightarrow$ )

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0, \text{ Let } \epsilon = -a, a + \epsilon = a + (-a) = 0 \leq 0$$

( $\Leftarrow$ )

$$a \geq 0, \epsilon$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

( $\Rightarrow$ )

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0, \text{ Let } \epsilon = -a, a + \epsilon = a + (-a) = 0 \leq 0$$

( $\Leftarrow$ )

$$a \geq 0, \epsilon > 0$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

( $\Rightarrow$ )

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0, \text{ Let } \epsilon = -a, a + \epsilon = a + (-a) = 0 \leq 0$$

( $\Leftarrow$ )

$$a \geq 0, \epsilon > 0, a + \epsilon$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

$(\Rightarrow)$

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0, \text{ Let } \epsilon = -a, a + \epsilon = a + (-a) = 0 \leq 0$$

$(\Leftarrow)$

$$a \geq 0, \epsilon > 0, a + \epsilon > 0$$

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Start

## Theorem

$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

## Proof.

( $\Rightarrow$ )

$$a < 0 \Rightarrow [\exists \epsilon > 0 \text{ s.t. } a + \epsilon \leq 0]$$

$$a < 0, \text{ Let } \epsilon = -a, a + \epsilon = a + (-a) = 0 \leq 0$$

( $\Leftarrow$ )

$$a \geq 0, \epsilon > 0, a + \epsilon > 0$$





$$[\forall \epsilon > 0, a + \epsilon > 0] \Leftrightarrow a \geq 0$$

▶ Home